

ΤΥΠΟΛΟΓΙΟ

| Κατανομή | Συνάρτηση μάζας πιθανότητας p_x (ΣΜΠ) Συνάρ. πυκνότητας πιθανότητας f_x (ΣΜΠ) | Παράμετροι | Μέση τιμή & διασπορά |
|----------|--|--------------|--|
| Poisson | $p_x(x) = \frac{(It)^x}{x!} e^{-It}$ | λ | $E(X) = \lambda x$ $Var(X) = \lambda x$ |
| Εκθετική | $f_x(x) = m e^{-mx}$ | μ | $E(X) = \mu$ $Var(X) = \mu^2$ |
| Γάμμα | $f_x(x) = e^{-\lambda x} \frac{\lambda^n x^{n-1}}{(n-1)!}$ | λ, n | $E(X) = n/\lambda$ $Var(X) = n/\lambda^2$ |

$$E[E(X|Y)] = E[X]$$

$$X(t) = \sum_{i=1}^{N(t)} Y_i \Rightarrow E[X(t)] = E[N(t)] \cdot E(Y_i), \quad Var[X(t)] = E[N(t)] \cdot E(Y_i^2)$$

M/M/1

$$r = \frac{l}{m}$$

$$p_0 = 1 - r$$

$$p_n = r^n (1 - r)$$

$$L = \frac{l}{m - l}$$

$$L_q = \frac{l^2}{m(m - l)}$$

$$L_q' = \frac{m}{m - l}$$

$$P\{Q \geq n\} = r^n$$

$$W_q(t) = \begin{cases} 1 - r, & t = 0 \\ 1 - r e^{-m(1-r)t}, & t > 0 \end{cases}$$

$$W_q = \frac{l}{m(m - l)}$$

$$w(t) = (m - l) e^{-(m-l)t}$$

$$W = \frac{1}{m - l}$$

$$L_q = l W_q$$

$$L = l W$$

$$L = L_q + \frac{l}{m}$$

$$W_q = \frac{L}{m}$$

M/M/1/K

$$p_0 = \begin{cases} \frac{1 - r}{1 - r^{K+1}}, & r \neq 1 \\ \frac{1}{K + 1}, & r = 1 \end{cases}$$

$$p_n = \begin{cases} \frac{(1 - r) r^n}{1 - r^{K+1}}, & r \neq 1 \\ \frac{1}{K + 1}, & r = 1 \end{cases}$$

$$p_0 = \frac{1}{1 + \sum_{n=1}^{\infty} \prod_{i=1}^n \frac{l_{i-1}}{m_i}}$$

$$p_n = p_0 \prod_{i=1}^n \frac{l_{i-1}}{m_i}$$

$$\boxed{\text{M/M/S}} \quad r = \frac{r}{S} = \frac{I}{Sm} \quad p_0 = \left[\sum_{n=0}^{S-1} \frac{r^n}{n!} + \frac{Sr^S}{S!(S-r)} \right]^{-1} \quad p_n = \begin{cases} \frac{I^n}{n!m^n} p_0, & 1 \leq n \leq S \\ \frac{I^n}{S^{n-S} S! m^n} p_0, & n \geq S \end{cases}$$

$$L_q = \frac{(I/m)^S I m}{(S-1)!(Sm-I)^2} p_0$$

$$W_q = \frac{(I/m)^S m}{(S-1)!(Sm-I)^2} p_0$$

$$L = \frac{(I/m)^S I m}{(S-1)!(Sm-I)^2} p_0 + \frac{I}{m}$$

$$W = \frac{(I/m)^S m}{(S-1)!(Sm-I)^2} p_0 + \frac{1}{m}$$

$$W_q(0) = 1 - \frac{S \left(\frac{I}{m} \right)^S}{S! \left(S - \frac{I}{m} \right)} p_0$$

$$W_q(t) = \frac{\left(\frac{I}{m} \right)^S (1 - e^{-(mS-1)t})}{(S-1)! \left(S - \frac{I}{m} \right)} p_0 + W_q(0)$$

 $\boxed{\text{M/M/S/K}}$

$$p_0 = \begin{cases} \left[\sum_{n=0}^{S-1} \frac{1}{n!} \left(\frac{I}{m} \right)^n + \frac{\left(\frac{I}{m} \right)^S}{S!} \cdot \frac{1 - \left(\frac{I}{Sm} \right)^{K-S+1}}{1 - \frac{I}{Sm}} \right]^{-1}, & \frac{I}{Sm} \neq 1 \\ \left[\sum_{n=0}^{S-1} \frac{1}{n!} \left(\frac{I}{m} \right)^n + \frac{\left(\frac{I}{m} \right)^S}{S!} \cdot (K-S+1) \right]^{-1}, & \frac{I}{Sm} = 1 \end{cases}$$

$$r = \frac{r}{S} = \frac{I}{Sm} \quad p_n = \begin{cases} \frac{1}{n!} \left(\frac{I}{m} \right)^n p_0, & 1 \leq n \leq S \\ \frac{1}{S^{n-S} S!} \left(\frac{I}{m} \right)^n p_0, & S \leq n \leq K \end{cases}$$

$$L_q = \frac{p_0 (Sr)^S}{S!(1-r)^2} r \left[1 - r^{K-S+1} - (1-r)(K-S+1)r^{K-S} \right] \quad W_q = \frac{L_q}{I'}, \text{ όπου } I' = I(1-p_k)$$

$$W = W_q + \frac{1}{m}$$

$$L = WI'$$

$$L = L_q + S - p_0 \sum_{n=0}^{S-1} \frac{(S-n)(rS)^n}{n!}$$

$$\boxed{\text{M/M/S/S}} \quad p_n = \frac{\frac{1}{n!} \left(\frac{I}{m} \right)^n}{\sum_{r=0}^S \frac{1}{r!} \left(\frac{I}{m} \right)^r}$$